

# Towards a unified EoS for quark-nuclear matter.

Abstract

The aim of our work is to develop a unified equation of state (EoS) for nuclear and quark matter for a wide range in temperature, density and isospin so that it becomes applicable for heavy-ion collisions as well as for the astrophysics of neutron stars, their mergers and supernova explosions [1]. As a first step, we use improved EoS for the hadronic and quark matter phases and join them via Maxwell construction. For this we work with a generalized density functional approach for the self energies in a quasi particle picture, which gives us the possibility to start with a reasonable physical basis and apply improvements to fit certain constraints from lattice QCD and neutron star measurements.

cluster expansion

• bound states are treated as new elementary particles

Phase transition

• first approach is Maxwell construction

# Towards CVE

- Cluster Virial Expansion with quarks as fundamental degrees of freedom and hadrons as bound states
- formulation for nuclear matter already done [2]

#### quasiparticles

• replacing interacting particles by system of free quasi particles

#### selfenergies shift energy dispertion relation

$$E_i^{\rm qu} = \sqrt{p^2 + (m-S)^2} + V$$

virial expantion between quasi clusters up to 2nd order

#### **CVE for quark matter**

• hadrons (baryons, mesons) are bound states of quarks • need proper inclusion of confinement  $\rightarrow$  density functional

# Density Functional Approach

• quasiparticle approach for grand potential

 $\omega = -g \int \frac{\mathrm{d}^3 p}{(2\pi)^3} \left\{ T \ln[1 + \mathrm{e}^{-(E - \tilde{\mu})/T}] + \dots \right\} - U \quad (5)$ 

• effectiv mass M = m - S and chemical potential  $\tilde{\mu} = \mu - V$ • scalar  $S = \Delta m + m^{R}$  and vector  $V = \Delta E + E^{R}$  selfenergies • mass and energy shifts can have arbitrary density dependence. • rearrangement contributions  $m^{\rm R}$ ,  $E^{\rm R}$  and U garantee thermodynamical consistency by reproducing the usual quasi particle form for the densities

$$n^{v} = g \int \frac{\mathrm{d}^{3} p}{(2\pi)^{3}} \left\{ \frac{1}{\mathrm{e}^{(E-\tilde{\mu})/T}} - \frac{1}{\mathrm{e}^{(E+\tilde{\mu})/T}} \right\}$$
(6)  
$$n^{s} = g \int \frac{\mathrm{d}^{3} p}{(2\pi)^{3}} \frac{M}{E} \left\{ \frac{1}{\mathrm{e}^{(E-\tilde{\mu})/T}} + \frac{1}{\mathrm{e}^{(E+\tilde{\mu})/T}} \right\}$$
(7)

• matching both EoS at point of chemical ( $\mu$ ) thermal (T) and mechanical (p) equilibrium.

• maxwell construction can't create a critical point!



Figure 2: PT for several temperaturs with density jump.



#### virial expansion

$$\beta p = \sum_{a} z_a + \sum_{ab} z_a z_b b_{ab} + \mathcal{O}(z^3)$$

with fugacity  $z_a = (2s+1)\Lambda_a^{-3}e^{\beta\mu_a}$ ;  $\Lambda_a^2 = 2\pi\beta/m_c$ ;

• The second  $b_{ab}$  virial coefficient by Beth-Uhlenbeck formula

$$b_{ab} = 8\pi^{3/2} \lambda_{ab}^3 \sum_{l} (2l+1) Z_{ab,l} + \delta_{ab} b_a^0$$

$$Z_{ab,l} = \sum_{n} e^{-\beta E_{ab}^{nl}} + \frac{1}{\pi} \int_0^\infty dE e^{-\beta E} \frac{d}{dE} \eta_{ab,l}(E) , \qquad (3)$$

with degeneracy expansion  $b_a^0 = \pm \Lambda_a/g_c 2^{-5/2}$ .



• dividing into bound and scattering contribution • replacing the particles by quasi-particles leads to absorbtion of scattering contribution in meanfield [3, 4]

$$Z_{ab,l}^{\text{scatt}} = \frac{1}{\pi} \int_0^\infty dE \ e^{-\beta E} \ 2\sin^2(\delta_l(E)) \frac{d\delta_l(E)}{dE}.$$
 (4)



## Two phase construction

• constructing phasetransition of two seperate models

(2)

(1)

#### **Hadron Phase**

- Nucleons via DD2 model [5]  $\rightarrow$  high density improvement via excluded volumen [6]
- Simplest ansatz of a hadron gas, including  $\pi$ ,  $\Lambda$  and K, with  $\mu_{\pi} = 0$ ;  $\mu_{\Lambda} = \mu_{B} - \mu_{S}$ ;  $\mu_{K^{0}} = \mu_{K^{+}} = \mu_{S}$ .
- determine  $\mu_{\rm S}$  to ensure net strange neutrality

 $0 = n_{\rm S} = -n_{\Lambda} + n_{\bar{\Lambda}} + n_{K^+} - n_{K^-} + n_{K^0} - n_{\bar{K}^0}$  (8)

### **Quark Phase**

- Quarks and Gluons with effective confinement mechanism [7]
- detailled information on poster of Mark Alexander Kaltenborn
- parameters are fit to satisfy lattice prediction for transition temperature for  $\mu_{\rm B} = 0$  and maximal neutron star mass.

Figure 3: Resulting phasediagram with quark-hadron phasetransition for symmetric matter.

# Outlook

- applying the results of the current EoS to simulations of heavy ion collisions and supernova explosions
- improving the PT construction by the approach of [8] to obtain critical point
- formulation and solution of the cluster virial expansion for quarkhadron matter

# References

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